# Selective Synthesis of Molecular Borromean Rings: Engineering of Supramolecular Topology via Coordination-Driven Self-Assembly 

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## Supporting Information


#### Abstract

Molecular Borromean rings (BRs) is one of the rare topology among interlocked molecules. Templatefree synthesis of BRs via coordination-driven self-assembly of tetracene-based $\mathrm{Ru}(\mathrm{II})$ acceptor and ditopic pyridyl donors is reported. NMR and single-crystal XRD analysis observed sequential transformation of a fully characterized monomeric rectangle to molecular BRs and vice versa. Crystal structure of BRs revealed that the particular topology was enforced by the appropriate geometry of the metallacycle and multiple parallel-displaced $\pi-\pi$ interactions between the donor and tetracene moiety of the acceptor. Computational studies based on density functional theory also supported the formation of BRs through dispersive intermolecular interactions in solution.


In the past two decades abiological self-assembly has emerged as a well-established method for the rational design of supramolecules by the independent pioneering work of Stang, ${ }^{1}$ Fujita, ${ }^{2}$ Raymond, ${ }^{3}$ Mirkin, ${ }^{4}$ and others ${ }^{5}$ using the metal-ligand coordination. The coordination-driven self-assembly approach is now competing and complimenting the covalent synthetic methods for realizing the topologically complicated fascinating molecular architectures. ${ }^{6}$ This approach is now being frequently used in the synthesis of commonly known threaded architectures such as catenanes, rotaxanes, and links. ${ }^{7-9}$ The synthesis of [2]catenanes has become routine, ${ }^{6}$ whereas the synthesis of more topologically complex, mechanically interlocked molecular architectures such as Borromean rings (BRs), ${ }^{10}$ Solomon link, ${ }^{11}$ star of David catenane, ${ }^{12}$ and pentafoil knots ${ }^{13}$ is still a great challenge. Molecular BRs consist of three chemically independent rings that are locked in such a way that no two of the three rings are linked with each other as a Hopf link and opening of any one ring unlinks all. ${ }^{14}$ Recently the configuration of BRs was selected for the new logo of International Mathematical Union. ${ }^{15}$ BRs topology has been previously observed in DNA ${ }^{16}$ and crystal packing, ${ }^{17}$ and BRs intermediates ${ }^{18}$ have also been reported. However, there are only two strategies known in the literature for the synthesis of discrete real (chemically nonconnected) molecular BRs. Stoddart reported the first BRs associated with six Zn (II) metal coordination, ${ }^{19}$ subsequent demetalation provided real BRs along with free and open rings. ${ }^{20}$ Jin reported another
strategy using $\mathrm{Cu}(\mathrm{II})$ derived acceptor to produce real and associated BRs. However, the presence of paramagnetic $\mathrm{Cu}(\mathrm{II})$ nuclei restricted their NMR analysis to studying their purity and interconversion to monomeric rectangles (Figure 1). ${ }^{21}$


Figure 1. Reported examples of BRs: (a) metal associated BRs, (b) real BRs after demetalation, (c) real BRs wearing paramagnetic Cu (II) ions.

With suitable modifications in the length, shape, and functionality of the donor, we recently reported the templatefree synthesis of a molecular Solomon link, ${ }^{22 a}$ a Hopfs link, ${ }^{22 b}$ an interlocked prismatic cage, ${ }^{22 \mathrm{c}}$ and a noncatenane "rectangle-in-rectangle" ${ }^{22 \mathrm{~d}}$ through the combined strategy of coordination driven self-assembly and $\pi-\pi$ stacking. Here we report the template-free self-assembly of BRs and solvent-induced sequential interconversion of BRs to a monomeric ring by carefully selecting the dimensions and functionality of the donor and acceptor. The BRs topology was obtained from the coordination-driven self-assembly of an arene-Ru(II) acceptor A and a ditopic ligand, 1,4-bis(4-pyridinylethynyl) benzene ( $\mathbf{L}_{1}$ ) (Scheme 1).
The stirring of a $1: 1$ mixture ( 0.5 mM ) of acceptor $\mathbf{A}$ and ligand $\mathrm{L}_{1}$ in $\mathrm{CD}_{3} \mathrm{OD}$ for 6 h at room temperature resulted in a clear greenish solution. The neat ${ }^{1} \mathrm{H}$ NMR spectrum of the solution clearly indicated the quantitative self-assembly of molecular rectangle 1 as $\alpha$ - and $\beta$-pyridyl protons were shifted from 8.67 and 7.55 ppm to 8.52 and 7.33 ppm , respectively (Figures 2 and S1-S2). Similarly, the phenylene protons (labeled as $\mathrm{H}_{\mathrm{L} 1}$ ) were also shifted to 7.30 ppm from 7.64 ppm in the $\mathbf{L}_{1}$. The prominent peaks at $m / z=742.76[1-3 \mathrm{OTf}]^{3+}$ in the ESI-MS analysis confirmed the formation of 1 , which were in good agreement with the theoretical isotopic distributions of

[^0]Scheme 1. Self-Assembly and Interconversion of BRs and Monomeric Rectangles


Figure 2. Partial ${ }^{1} \mathrm{H}$ NMR in $\mathrm{CD}_{3} \mathrm{OD}$ of (a) donor (b) self-assembled monomeric rectangle $\mathbf{1}[0.5 \mathrm{mM}]$, (c) mixture of $\mathbf{1}$ and Rs 2 [3.0 $\mathrm{mM}]$, (d) ${ }^{1} \mathrm{H}$ DOSY NMR of $\mathbf{1}[0.5 \mathrm{mM}]$, and (e) ${ }^{1} \mathrm{H}$ DOSY NMR of $\mathbf{1}+\mathbf{2}[3.0 \mathrm{mM}]$.

1 (Figure S3). Upon increasing the reaction concentration to 1.0 mM , new peaks were observed along with peaks from 1 in the ${ }^{1} \mathrm{H}$ NMR spectrum that indicated the formation of a new compound (Figure 5S). The similar reaction in $\mathrm{CD}_{3} \mathrm{NO}_{2}$ also resulted in only 1 unaffected by concentration (Figure S2). This observation prompted us to carry out reactions in $\mathrm{CD}_{3} \mathrm{OD}$ in various concentrations from 0.5 to 8.0 mM (solubility was poor beyond 6.0 mM ) (Figure S5). The reaction carried out at 6.0 mM provided the maximum concentration (56\%) of the new compound. The ${ }^{1} \mathrm{H}$ NMR spectral pattern of new compound was similar to that of $\mathbf{1}$ except for the fact that the phenylene protons (labeled as $\mathrm{H}_{\mathrm{L}}$ ) were highly shifted upfield from 7.64 to 4.77 ppm (Figure 2).

The prominent peaks in the ESI-MS spectrum at $\mathrm{m} / \mathrm{z}=$ $2525.86[2-3 \mathrm{OTf}]^{3+}$ and the perfect agreement with the theoretical isotopic distributions confirmed the presence of BR 2 (Figure S6). The structures of Rs 2 and monomeric rectangle 1 were confirmed in solution by DOSY, ROESY,

HSQC, and HMBC 2D NMR (Figures S1-S19) combined with ESI-MS analysis. The strong upfield shift of phenylene protons in the ${ }^{1} \mathrm{H}$ NMR spectrum was a result of paralleldisplaced $\pi-\pi$ stacking with the tetracene moiety of acceptor $\mathbf{A}$ and $\mathrm{CH} \cdots \pi$ interactions with the pyridyl ring of another rectangle. The DOSY NMR spectrum of $\mathbf{1}[0.5 \mathrm{mM}]$ in $\mathrm{CD}_{3} \mathrm{OD}$ was recorded and revealed a diffusion coefficient ( $D$ ) of $5.3 \times 10^{-10} \mathrm{~m}^{2} \mathrm{~s}^{-1}$. The DOSY NMR spectrum of mixture of $\mathbf{1}+\mathbf{2}[3.0 \mathrm{mM}]$ in $\mathrm{CD}_{3} \mathrm{OD}$ also confirmed the NMR signals associated with two diffusion coefficients at $D=5.1 \times 10^{-10} \mathrm{~m}^{2}$ $\mathrm{s}^{-1}$ for $\mathbf{1}$ and $3.9 \times 10^{-10} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ for 2 (Figures 2 and S10-S13). The ${ }^{1} \mathrm{H}-{ }^{1} \mathrm{H}$ ROSEY spectra of $\mathbf{1}[0.5 \mathrm{mM}]$ and $\mathbf{1}+\mathbf{2}$ [3.0 $\mathrm{mM}]$ in $\mathrm{CD}_{3} \mathrm{OD}$ also showed all the possible coupling interactions in the structure of 1 and BRs 2 . The coupling interactions of phenylene protons of donors with $\alpha$-, $\beta$-tetracene protons of acceptor moiety were also observed, which was possible only in the case of BR topology of 2 (Figures S14S15).

To identify the driving forces behind the formation of ERs, we tried the self-assembly of ligand $\mathbf{L}_{\mathbf{1}}$ with other similar acceptors, ${ }^{22 a}$ but none of them resulted in BRs topology. In search of replacing $L_{1}$ to get increased yield, we tried various ligands and found 2,5-bis(4-pyridinylethynyl)thiophene ( $\mathbf{L}_{2}$ ) provided much better yield up to $65 \%$ of Rs. Ligand $\mathbf{L}_{1}$ was replaced with $\mathbf{L}_{2}$ in identical reactions which earlier produced 1 and 2 , resulting in the formation of new compounds 3 and 4. The combined NMR study and prominent peaks at $m / z=$ 746.73 [3-3OTf $^{3+}$ and $m / z=1463.53[4-5 O T f]^{5+}$ in the ESIMS analysis confirmed the formation of monorectangle 3 and BR 4, which were in good agreement with their theoretical isotopic distributions (Figures S20-S37). In the search of getting pure Rs, we tried the self-assembly in different solvents and mixtures of solvents in which $\mathbf{3}$ and $\mathbf{4}$ were soluble. Only $\mathrm{D}_{2} \mathrm{O}$ added in $\mathrm{CD}_{3} \mathrm{OD}$ solution provided improved yield of BRas. The 6.0 mM reaction mixture in $\mathrm{CD}_{3} \mathrm{OD}$ was stirred for 6 $h$, and then from this solution six different sets of reactions were prepared by adding $\mathrm{D}_{2} \mathrm{O}$ and adjusting the $\mathrm{CD}_{3} \mathrm{OD}: \mathrm{D}_{2} \mathrm{O}$ ratio up to 9:6 (up to allowed solubility). The resulting reaction mixtures were further stirred for 6 h , and ${ }^{1} \mathrm{H}$ NMR was recorded (Figure 3). The NMR spectra showed a gradual increase in the percentage of ERs upon addition of $\mathrm{D}_{2} \mathrm{O}$, which increased up to $87 \%$ in the $\mathrm{CD}_{3} \mathrm{OD}: \mathrm{D}_{2} \mathrm{O}$ ratio of 9:6.

The DOSY NMR spectrum of mixture of $\mathbf{3 + 4}[4.0 \mathrm{mM}]$ in $\mathrm{CD}_{3} \mathrm{OD}$ also revealed two diffusion coefficients at $D=5.5 \times$


Figure 3. Partial ${ }^{1} \mathrm{H}$ NMR spectra of mixture of $\mathbf{3 + 4}$ in $\mathrm{CD}_{3} \mathrm{OD}[6.0$ mM ] showing transformation to $87 \%$ of Rs 4 upon increasing the $\mathrm{CD}_{3} \mathrm{OD}: \mathrm{D}_{2} \mathrm{O}$ ratio up to 9:6.
$10^{-10} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ for 3 and $4.2 \times 10^{-10} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ for 4 , whereas DOSY NMR of 4 obtained in $\mathrm{CD}_{3} \mathrm{OD}: \mathrm{D}_{2} \mathrm{O}$ (9:6) showed the diffusion coefficient at $D=1.5 \times 10^{-10} \mathrm{~m}^{2} \mathrm{~s}^{-1}$ for NMR signals associated with BRs 4 (Figures S27-S30). The coupling interactions of $\beta$-thiophene protons of donors with $\alpha-, \beta$ tetracene protons of acceptor moiety in the ${ }^{1} \mathrm{H}-{ }^{1} \mathrm{H}$ ROSEY spectra of $3+4[4.0 \mathrm{mM}]$ in $\mathrm{CD}_{3} \mathrm{OD}$ were also observed to confirm BRs topology of 4 (Figures S31 and S32). The transformation of monorectangle 3 to BRs 4 upon sequential addition of $\mathrm{D}_{2} \mathrm{O}$ was probably instigated by the hydrophobic effect. The metallacycles due to the presence of hydrophobic moieties would come closer to reduce the solvent accessible surface area in order to avoid exposure to $\mathrm{D}_{2} \mathrm{O}$. Computational calculations of solvent effect also suggested a decrease in solvent accessible surface area by $\sim 172 \AA^{2}$ due to the formation of BRs 2 (SI).

To understand the role of $\pi-\pi$ interactions in formation of BRs, 0.5-8.0 equiv of pyrene was added to the previously prepared 4.0 mM solutions of $\mathbf{1}+\mathbf{2}$ and $\mathbf{3}+\mathbf{4}$ in $\mathrm{CD}_{3} \mathrm{OD}$. The resulting reaction mixtures were further stirred for 2 h at $45^{\circ} \mathrm{C}$, and NMR was recorded. The NMR data clearly show the gradual transformation of BRs to single rectangle upon increasing the concentration of pyrene (Figures S38 and S39). The BRs completely transformed into single rectangles by interacting with 8.0 equiv of pyrene. Solution of $3+4$ in $\mathrm{CD}_{3} \mathrm{OD}$ upon sequential dilution with $\mathrm{CD}_{3} \mathrm{OD}$ was also resulted in pure monomeric rectangle 3 (Figures S40).

The single-crystal X-ray diffraction (scXRD) analysis unambiguously confirmed the structures of $\mathbf{1}$ encapsulated with two molecules of pyrene, 3 (obtained from the $\mathrm{CD}_{3} \mathrm{NO}_{2}$ solution), and BRs 2 and 4 in the solid state (Figure 4).


Figure 4. X-ray crystal structures of (a) $1 \supset$ (2•pyrene), (b) 3, (c) 2, and (d) 4. Hydrogen atoms and counteranions are omitted for clarity.

Considering the metallacycles as rectangles, the scXRD analysis confirmed the molecular structure of 2 with pyritohedral symmetry $\left(T_{h}\right)$, wherein the three rings were found to be linked with the topology of BRs. Each of the three equivalent rings adopted a distorted rectangle-like conformation with an average length and width ( $\mathrm{Ru}-\mathrm{Ru}$ distance) of 20.1 and $8.1 \AA$ respectively. The three chemically nonconnected distorted rectangles were held together by $\mathrm{CH} \cdots \pi$ ( $2.9 \AA$ ) interactions and multiple parallel-displaced $\pi-\pi$ (3.5 $\AA$ ) interactions between phenyl-ethynyl-pyridinyl moieties of the donor and tetracene moieties of the acceptor (Figure S44-S45). The structure of 4 was also found similar to BRs 2 with average
rectangular dimensions of 19.6 and $7.9 \AA$. In the structure of $\mathbf{1}$, two pyrene molecules were found to be encapsulated and strongly interacted with the ethynyl-pyridinyl moiety stabilized via parallel-displaced $\pi-\pi$ stacking ( $3.5 \AA$ ) and via CH $\cdots \pi$ ( 2.7 $\AA$ ) interactions in edge-to-face fashion with the tetracene moiety of the acceptor. Interestingly, the donor moieties of the rectangle were curved outside in the case of BRs 2 and 4, slightly toward the inside in $1 \supset(2$-pyrene $)$, and almost straight in the case of monomeric rectangle 3 (Figures S42-S48). This observation clearly indicated that the driving forces in the formation of BRs are multiple $\pi-\pi$ and $\mathrm{CH} \cdots \pi$ interactions, which is also supported by the theoretically obtained spatial distribution of noncovalent interaction (NCI) by plotting the iso-surfaces of reduced density gradient as shown in Figure S49. ${ }^{23}$

In conclusion, template-free synthesis of molecular BRs was achieved via coordination-driven self-assembly and paralleldisplaced $\pi-\pi$ stacking of aromatic rings. Various acceptors and donors in different solvents and combination of solvents were tried, but tetracene-based acceptor and thiophene-derived donor in methanol-water solution were found to be the best combination to get the desired topology. The self-assembly in nitromethane resulted only in monomeric rectangle regardless of concentration. In methanol, whereas only a single rectangle was obtained in dilute reaction condition, BRs gradually started forming upon increasing the reaction concentration beyond 1.0 mM . The formation of BRs was inhibited by the presence of $\pi$ -electron-rich pyrene template shown by NMR analysis and Xray crystal structure of the monomeric rectangle encapsulated with pyrene. The real molecular BRs were characterized by scXRD analysis in solid-state along with elegant demonstration of linking and unlinking by NMR analysis in solution. When all the NMR, scXRD, and computational studies were combined, the driving forces for the formation of BRs were found to be CH $\cdots \pi$ interactions and multiple parallel-displaced $\pi-\pi$ interactions with appropriate geometry of donor and acceptor. We demonstrated the engineering of complex supramolecular topology through controlling concentration, solvent, template, and the functionality of donor and acceptor.

## ASSOCIATED CONTENT

## (s) Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.6b04545.

Details of the synthesis, spectroscopic data, and computation details for $\mathbf{1 - 4}$ (PDF)
Crystallographic data (CIF)

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## Notes

The authors declare no competing financial interest.

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(23) DFT computations were performed to study the intermolecular interactions in BRs 2. The binding energies (BE) evaluated using three different hybrid functionals were -127.8 ( $\omega$ B97X-D), -58.9 (M062X), and $26.6 \mathrm{kcal} / \mathrm{mol}$ (PBEO), with the geometry determined by scXRD. The variation of BE of employed methods, according to the performance in describing NCI, clearly indicates that the NCI plays a crucial role in the formation of BRs (see SI for computation details).


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